

Structural Engineering Justification

Project Type: Side Extension
Client Name: -
Address: -
General Comments:

Revision: v1

Section Summary

Section	Size	Material Grade	Connection
Floor Joists	1 No. 225 x 50mm	Timber Grade C16	Approved flooring to be spiked to every floor joist.
Timber Rafters	1 No. 150 x 50mm	Timber Grade C16	Spiked to wall plate & ridge board.
Beam A	305 x 165 x 54 kg/m UB	Grade S275 UB	Sliced connection - see detail.
Beam B	356 x 171 x 51 kg/m UB	Grade S275 UB	Sliced connection - see detail.
Roof Trimmer	3 No. 225 x 50mm	Timber Grade C16	50 mm DS toothed plate connector with M10 bolts at 400 mm c/c's.

Imposed loadings are in accordance with BS6399-1:1996 Loading for buildings.

Roof

Dead Load **0.85** kN/m²
Imposed Load **0.85** kN/m²

Ceiling

Dead Load **0.25** kN/m²
Imposed Load **0.25** kN/m²

Floor

Dead Load **0.50** kN/m²
Imposed Load **1.50** kN/m²

Walls

Partitions **0.50** kN/m²
Blockwork (100) **1.80** kN/m²
Brickwork (112.5) **2.50** kN/m²

Floor Joist Design

(BS5268-2:2002)

Max opening span	L = 4.2	m
Floor Dead Load DL	DL = 0.50	kN/m ²
Floor Live Load LL	LL = 1.50	kN/m ²
Joist spacing S	S = 0.40	m

$$\begin{aligned} \text{Joist Dead Load } w_d &= S \times DL \\ &= \mathbf{0.20} \quad \text{kN/m} \end{aligned}$$

$$\begin{aligned} \text{Joist Live Load } w_l &= S \times LL \\ &= \mathbf{0.60} \quad \text{kN/m} \end{aligned}$$

$$\text{Joist self weight } F_j = \mathbf{0.15} \quad \text{kN/m}$$

$$\text{Total Service Load} = \mathbf{0.95} \quad \text{kN/m}$$

$$\begin{aligned} R_a = R_b = W / 2 &= 0.95 \quad \times L / 2 \\ &= \mathbf{2.00} \quad \text{kN} \end{aligned}$$

$$\begin{aligned} BM_{\max} &= W L / 8 \\ &= \mathbf{2.09} \quad \text{kN/m} \end{aligned}$$

Consider long term uniformly distributed load

$$\text{Load duration factor} \quad K_3 = \mathbf{1.00}$$

Modification factors

$$\begin{aligned} \text{Section depth factor} \quad K_7 &= (300 / h)^{0.11} \\ &= \mathbf{1.03} \end{aligned}$$

$$\text{Load sharing factor} \quad K_8 = \mathbf{1.10}$$

Bending stress

$$\text{Bending stress} \quad \sigma_m = \mathbf{5.30} \quad \text{N/mm}^2 \quad (\text{Class C16 BS5268:Part2:2002})$$

Permissible bending stress

$$\begin{aligned} \sigma_{m_adm} &= \sigma_m \times K_3 \times K_7 \times K_8 \\ &= \mathbf{6.00} \quad \text{N/mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Z required} \quad Z &= BM_{\max} / \sigma_{m_adm} \\ &= \mathbf{349} \quad \text{cm}^3 \end{aligned}$$

Specified Joist details

Joist breadth	$b = 50$	mm	(Class C16 BS5268:Part2:2002)
Joist depth	$h = 225$	mm	
Joist spacing	$s = 400$	mm	
Joist span	$L = 5300$	mm	
Modulus of elasticity	$E_{\text{mean}} = 8800$	N/mm ²	SEPB P128
Strength Class C16 Timber (BS5268:Pt 2:2002)			

Section properties

Second moment of area $I = b \times h^3 / 12$
 $= 47460938 \text{ mm}^4$

Section modulus $Z = b \times h^2 / 6$
 $= 421875 \text{ mm}^3$

Applied bending stress
 $\sigma_{\text{m_max}} = \text{BM} / Z$
 $= 4.97 \text{ N/mm}^2$

OK - Applied bending stress within permissible limits of: 6.00 N/mm²

Check shear stress

Shear stress $\tau = 0.67 \text{ N/mm}^2$ SEPB P128
(Class C16 BS5268:Part2:2002)

Permissible shear stress
 $\tau_{\text{adm}} = \tau \times K_3 \times K_8$
 $= 0.737 \text{ N/mm}^2$

Applied shear stress
 $\tau_{\text{max}} = 3 \times W \times L / (4 \times b \times h)$
 $= 0.34 \text{ N/mm}^2$

OK - Applied shear stress within permissible limits of: 0.737 N/mm²

Check deflection

Permissible deflection $\delta_{\text{adm}} = \min(0.003 \times L)$
 $= 15.9$ (should not be greater than 14 mm)
 $= 14 \text{ mm}$

Maximum deflection $\delta_{\text{max}} = 5 \times W \times L^3 / 384 \times E_{\text{mean}} \times I$
 $= 4.41 \text{ mm}$

OK - Actual deflection within permissible limits of: 14 mm

Therefore use 225mm x 50mm C16 joists @ 400c/c's

Timber Rafters

(BS5268-2:2002)

Roof Dead Load DL	DL = 0.85	kN/m ²
Roof Live Load LL	LL = 0.85	kN/m ²
Ceiling Dead Load	DL = 0.25	kN/m ²
Ceiling Live Load	LL = 0.25	kN/m ²
Rafter spacing S	S = 0.40	m
Roof pitch	PR = 33.0	Deg
Length	RLR = 3.20	m

$$\begin{aligned} \text{Roof Dead Load} &= 0.85 / \cos(\text{PR}) \\ &= \mathbf{1.01} \quad \text{kN/m} \end{aligned}$$

$$\text{Roof Live Load} = \mathbf{0.85} \quad \text{kN/m}$$

$$\text{Joist self weight Fj} = \mathbf{0.15} \quad \text{kN/m}$$

$$\begin{aligned} \text{Ceiling Dead Load} &= S \times \text{DL} \\ &= \mathbf{0.10} \quad \text{kN/m} \end{aligned}$$

$$\begin{aligned} \text{Ceiling Live Load} &= S \times \text{LL} \\ &= \mathbf{0.10} \quad \text{kN/m} \end{aligned}$$

$$\mathbf{UDL Total Service Load} = \mathbf{2.21} \quad \text{kN/m}$$

$$\text{Ra} = \text{Rb} = W / 2 = \mathbf{1.42} \quad \text{kN}$$

$$\text{BMmax} = W L / 8 = \mathbf{1.81} \quad \text{kNm}$$

Consider long term uniformly distributed load

$$\text{Load duration factor} \quad K_3 = \mathbf{1.00}$$

Modification factors

$$\begin{aligned} \text{Section depth factor} \quad K_7 &= (300 / h)^{0.11} \\ &= \mathbf{1.03} \end{aligned}$$

$$\text{Load sharing factor} \quad K_8 = \mathbf{1.10}$$

Bending stress

$$\begin{aligned} \text{Bending stress} \quad \sigma_m &= \mathbf{5.30} \quad \text{N/mm}^2 \quad \text{SEPB P128} \\ &\quad \text{(Class C16 BS5268:Part2:2002)} \end{aligned}$$

Permissible bending stress

$$\begin{aligned} \sigma_{m_adm} &= \sigma_m \times K_3 \times K_7 \times K_8 \\ &= \mathbf{6.00} \quad \text{N/mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Z required} \quad Z &= \text{BM}_{\max} / \sigma_{m_adm} \\ &= \mathbf{302} \quad \text{cm}^3 \end{aligned}$$

Specified Joist details

Joist breadth	$b = 50$	mm	(Class C16 BS5268:Part2:2002)
Joist depth	$h = 150$	mm	
Joist spacing	$s = 400$	mm	
Joist span	$L = 3200$	mm	
Modulus of elasticity	$E_{\text{mean}} = 8800$	N/mm ²	SEP B P128
Strength Class C16 Timber (BS5268:Pt 2:2002)			

Section properties

Second moment of area $I = b \times h^3 / 12$
 $= 14062500$ mm⁴

Section modulus $Z = b \times h^2 / 6$
 $= 187500$ mm³

Applied bending stress

$$\sigma_{\text{m_max}} = \text{BM} / Z$$
$$= 9.67 \text{ N/mm}^2$$

**OK - Applied bending stress
within permissible limits of:**

$$6.00 \text{ N/mm}^2$$

Check shear stress

Shear stress $\tau = 0.67$ N/mm² SEP B P128
(Class C16 BS5268:Part2:2002)

Permissible shear stress

$$\tau_{\text{adm}} = \tau \times K_3 \times K_8$$
$$= 0.737 \text{ N/mm}^2$$

Applied shear stress

$$\tau_{\text{max}} = 3 \times W \times L / (4 \times b \times h)$$
$$= 0.71 \text{ N/mm}^2$$

**OK - Applied shear stress
within permissible limits of:**

$$0.737 \text{ N/mm}^2$$

Check deflection

Permissible deflection $\delta_{\text{adm}} = \min(0.003 \times L)$
 $= 9.6$ mm (maximum of 14 mm)

Maximum deflection $\delta_{\text{max}} = 5 \times W \times L^3 / 384 \times E_{\text{mean}} \times I$
 $= 7.63$ mm

**OK - Actual deflection
within permissible limits of:**

$$9.6 \text{ mm}$$

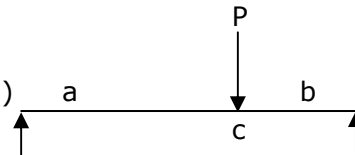
Therefore use 50mm x 150mm C16 timbers.

2 No. Rafters either side of Velux window locations.



Beam A
with UDL & Point Load from Trimmer

(BS5950 Part 1: 2000)



Max opening span	L = 7.00	m
Spacing	S = 4.00	m
Floor Dead Load DL	DL = 0.50	kN/m ²
Floor Live Load LL	LL = 1.50	kN/m ²
Wall Dead Load DL	DL = 2.50	kN/m ²
Wall Height	H = 3.20	m
Roof pitch	PR = 32.5	Deg
Length - wall to ridge	RLR = 3.00	m
Length - wall to eave	RLE = 1.00	m

Floor Dead Load wd = 0.5 x L x DL
= **1.75** kN/m

Floor Live Load w_l = 0.5 x L x LL
= **5.25** kN/m

Wall Dead Load = DL x Wall Height
= **8.00**

Beam self weight F_j = **0.25** kN/m

UDL Total Service Load = **15.25** kN/m

UDL - Design Load (w) = 1.5 x UDL
= **22.88** kN/m

Point Load from Trimmer = **2.00** kN

Point Design Load - (P) = 1.5 x P
= **3.00** kN

Distance a = **3.50** m

Distance b = **2.50** m

R_b = (Pb + wL x L/2) / 4
= **42.78** kN

W Total (Ra + Rb) = wL + P
= **163.13** kN

R_a = W - R_b
= **120.34** kN

BM under point load P = Pab / L
= **3.75** kNm

BM due to UDL = W L / 8
= **140.11** kNm

BM Total = **143.86** kNm

P_y = **275** N/mm²
(BS5950 Part 1:2000 Table 9 for Grade S275 steel)

$$\begin{aligned}
 S_x \text{ Required} &= BM / P_y \\
 &= \mathbf{523.13} \quad \text{cm}^3 \\
 I \text{ required} &= S \times W \times L^3 \\
 &= \mathbf{22381} \quad \text{cm}^3 \\
 \text{Max Deflection} &= L / 360 \\
 &= \mathbf{19.44} \quad \text{mm} \\
 L_e &= 1.0 \times L \\
 &= \mathbf{7000} \quad \text{mm}
 \end{aligned}$$

Try **305 x 165 x 54 kg/m UB** (SEPB P214)

$$\begin{aligned}
 \text{Section Depth} &= \mathbf{310.4} \quad \text{mm} \\
 \text{Flange Thickness (t)} &= \mathbf{7.9} \quad \text{mm} \\
 \text{Beam } S_x &= \mathbf{846.0}
 \end{aligned}$$

$$\begin{aligned}
 \text{Second moment of area} &= I_x \\
 &= \mathbf{11700} \quad \text{cm}^4
 \end{aligned}$$

OK - Actual beam greater than require limit of: $22381 \quad \text{cm}^3$

$$\begin{aligned}
 \text{Minor axis slenderness (h)} &= L_e / r_y \\
 &= \mathbf{201} \\
 x &= \text{Depth} / \text{Thickness} \\
 &= \mathbf{39.29}
 \end{aligned}$$

$$\begin{aligned}
 h / x &= \mathbf{5.12} \\
 \text{Slenderness factor (V)} &= \mathbf{0.79} \quad \text{BS5950:Table 14}
 \end{aligned}$$

$$\begin{aligned}
 \text{Slenderness correction factor (n)} \\
 &= \mathbf{1.0}
 \end{aligned}$$

$$\text{Buckling parameter (u)} = \mathbf{0.89}$$

$$\begin{aligned}
 \text{Lateral torsional buckling (hLT)} \\
 &= n \times u \times V \times h \\
 &= \mathbf{141.43}
 \end{aligned}$$

$$P_b = 107.74 \quad \text{N/mm}^2 \quad \text{BS5950:Table 11}$$

$$\begin{aligned}
 \text{Buckling resistance moment (M}_b) \\
 &= S_x \times P_b \\
 &= \mathbf{91.1} \quad \text{kNm}
 \end{aligned}$$

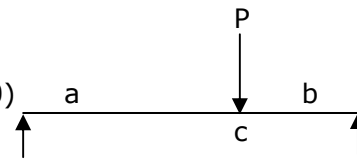
OK - Actual beam greater than require limit of: $143.86 \quad \text{kNm}$

Therefore use **305 x 165 x 54 kg/m UB** as Beam A.

Beam B

(BS5950 Part 1: 2000)

with UDL & Point Load from Beam A



Max opening span	L = 4.50	m
Spacing	S = 6.00	m
Floor Dead Load DL	DL = 0.50	kN/m ²
Floor Live Load LL	LL = 1.50	kN/m ²
Wall Dead Load DL	DL = 2.50	kN/m ²
Wall Height	H = 3.20	m
Roof pitch	PR = 32.5	Deg
Length - wall to ridge	RLR = 3.00	m
Length - wall to eave	RLE = 1.00	m
Roof Dead Load	= ((0.85 / cos(RP) x (RLR + RLE/2))	
	= 3.53	kN/m
Roof Live Load	= (0.85 x (RLR + RLE/2))	
	= 5.31	kN/m
Wall Dead Load	= DL x Wall Height	
	= 8.00	
Beam self weight Fj	= 0.25	kN/m
UDL Total Service Load	= 17.09	kN/m
UDL - Design Load (w)	= 1.5 x UDL	
	= 25.63	kN/m
Point Load from Beam A	= 81.57	kN
Point Design Load - (P)	= 81.57	kN
Distance a	= 4.00	m
Distance b	= 0.50	m
Rb	= (Pb + wL x L/2) / 4	
	= 39.60	kN
W Total (Ra + Rb)	= wL + P	
	= 196.92	kN
Ra	= W - Rb	
	= 157.32	kN
BM under point load P	= Pab / L	
	= 36.25	kN
BM due to UDL	= W L / 8	
	= 64.89	kNm
BM Total	= 101.14	kNm
Py	= 275	N/mm ²
	(BS5950 Part 1:2000 Table 9 for Grade S275 steel)	

$$\begin{aligned}
 S_x \text{ Required} &= BM / P_y \\
 &= \mathbf{367.78} \quad \text{cm}^3 \\
 I \text{ required} &= S \times W \times L^3 \\
 &= \mathbf{10767} \quad \text{cm}^3 \\
 \text{Max Deflection} &= L / 360 \\
 &= \mathbf{12.50} \quad \text{mm} \\
 L_e &= 1.0 \times L \\
 &= \mathbf{4500} \quad \text{mm}
 \end{aligned}$$

Try **356 x 171 x 51 kg/m UB** (SEPB P214)

$$\begin{aligned}
 \text{Section Depth} &= \mathbf{355.0} \quad \text{mm} \\
 \text{Flange Thickness (t)} &= \mathbf{7.4} \quad \text{mm} \\
 \text{Beam } S_x &= \mathbf{896.0}
 \end{aligned}$$

$$\begin{aligned}
 \text{Second moment of area} &= I_x \\
 &= \mathbf{14140} \quad \text{cm}^4
 \end{aligned}$$

OK - Actual beam greater than require limit of: $10767 \quad \text{cm}^3$

$$\begin{aligned}
 \text{Minor axis slenderness (h)} &= L_e / r_y \\
 &= \mathbf{129} \\
 x &= \text{Depth / Thickness} \\
 &= \mathbf{47.97}
 \end{aligned}$$

$$h / x = \mathbf{2.70}$$

$$\text{Slenderness factor (V)} = \mathbf{0.79} \quad \text{BS5950:Table 14}$$

$$\text{Slenderness correction factor (n)} = \mathbf{1.0}$$

$$\text{Buckling parameter (u)} = \mathbf{0.89}$$

$$\begin{aligned}
 \text{Lateral torsional buckling (hLT)} &= n \times u \times V \times h \\
 &= \mathbf{90.92}
 \end{aligned}$$

$$P_b = 107.74 \quad \text{N/mm}^2 \quad \text{BS5950:Table 11}$$

$$\begin{aligned}
 \text{Buckling resistance moment (Mb)} &= S_x \times P_b \\
 &= \mathbf{96.5} \quad \text{kNm}
 \end{aligned}$$

OK - Actual beam greater than require limit of: $101.14 \quad \text{kNm}$

Therefore use **356 x 171 x 51 kg/m UB** as Beam B.

Roof Trimmer

(BS5268-2:2002)

Max opening span	L = 4.00	m
Joist spacing S	S = 3.00	m
Roof pitch	PR = 33.0	Deg
Length - wall to ridge	RLR = 3.00	m
Roof Dead Load	= ((0.85 / cos(RP) x (RLR + RLE/2)) x 0.4 = 1.22	kN/m
Roof Live Load	= (0.85 x (RLR + RLE/2)) x 0.4 = 1.02	kN/m
Joist self weight Fj	= 0.15	kN/m
Total Service Load	= 2.39	kN/m
Ra = Rb = W / 2	= 2.39 = 4.77	x L / 2 kN
BM _{max}	= W L / 8 = 4.77	kN/m

Consider long term uniformly distributed load

Load duration factor $K_3 = \mathbf{1.00}$

Modification factors

Section depth factor $K_7 = (300 / h)^{0.11}$
= **1.03**

Load sharing factor $K_8 = \mathbf{1.10}$

Bending stress

Bending stress $\sigma_m = \mathbf{5.30}$ N/mm² (Class C16 BS5268:Part2:2002)

Permissible bending stress

$$\begin{aligned}\sigma_{m_adm} &= \sigma_m \times K_3 \times K_7 \times K_8 \\ &= \mathbf{6.00} \text{ N/mm}^2\end{aligned}$$

Z required $Z = BM_{max} / \sigma_{m_adm}$
= **795** cm³

Specified Joist details

Joist breadth	$b = 150$	mm	(Class C16 BS5268:Part2:2002)
Joist depth	$h = 225$	mm	
Joist spacing	$s = 400$	mm	
Joist span	$L = 4800$	mm	
Modulus of elasticity	$E_{\text{mean}} = 8800$	N/mm ²	SEPB P128
Strength Class C16 Timber (BS5268:Pt 2:2002)			

Section properties

Second moment of area $I = b \times h^3 / 12$
 $= #####$ mm⁴

Section modulus $Z = b \times h^2 / 6$
 $= 1265625$ mm³

Applied bending stress
 $\sigma_{\text{m_max}} = \text{BM} / Z$
 $= 3.77$ N/mm²

OK - Applied bending stress within permissible limits of: 6.00 N/mm²

Check shear stress

Shear stress $\tau = 0.67$ N/mm² SEPB P128
(Class C16 BS5268:Part2:2002)

Permissible shear stress
 $\tau_{\text{adm}} = \tau \times K_3 \times K_8$
 $= 0.737$ N/mm²

Applied shear stress
 $\tau_{\text{max}} = 3 \times W \times L / (4 \times b \times h)$
 $= 0.25$ N/mm²

OK - Applied shear stress within permissible limits of: 0.737 N/mm²

Check deflection

Permissible deflection $\delta_{\text{adm}} = \min(0.003 \times L)$
 $= 14.4$ (should not be greater than 14 mm)
 $= 14$ mm

Maximum deflection $\delta_{\text{max}} = 5 \times W \times L^3 / 384 \times E_{\text{mean}} \times I$
 $= 2.74$ mm

OK - Actual deflection within permissible limits of: 14 mm

Therefore use 3no. 225 x 50mm C16 timbers

Sections to be connected together using 50 mm DS toothed plate connector with M10 bolts at 400 mm c/c's.